

# ATTENDING TO TEACHER PREPARATION OUTCOMES FROM THE BEGINNING: LEARNING FROM BASELINE AND MID-PROGRAM ASSESSMENTS

Timothy Boerst, Meghan Shaughnessy,  
Deborah Loewenberg Ball, & Susanna Owens Farmer

AMTE 2015, Orlando, FL  
February 12, 2015



SCHOOL OF  
EDUCATION  
UNIVERSITY OF MICHIGAN

The research reported here was supported by the National Science Foundation, through a grant to the University of Michigan. The opinions, findings, and recommendations expressed are those of the authors and do not represent views of the National Science Foundation.



This work is licensed under the Creative Commons Attribution-NonCommercial-No Derivative Works  
Version 3.0 United States License: <http://creativecommons.org/licenses/by-nc-nd/3.0/us/>

© 2015 Mathematics Teaching and Learning to Teach • School of Education • University of Michigan • Ann Arbor, MI 48109 • [mtt@umich.edu](mailto:mtt@umich.edu)

# CHALLENGES FOR TEACHER PREPARATION

- Students, families, and schools need beginning teachers who are ready for classroom practice
- Teacher education needs to focus on core practices of teaching (Ball & Forzani, 2009; Grossman et al., 2009; Lampert & Graziani, 2009)
- Teacher educators would benefit from knowing more about the knowledge and skills that candidates bring to teacher preparation

# ORIENTING PROFESSIONAL PREPARATION TO WHAT TEACHER CANDIDATES BRING

If we knew more about the skills of those entering teacher education, we could reconsider:

- The curriculum (things that need to be learned and “unlearned”)
- Settings for teacher learning and needed resources
- Recruitment

We could also better track on their developing skill.

# LEARNING WHAT CANDIDATES BRING

- To have such information, we must assess practice: actual skills and knowledge for doing teaching
- Information gathered must:
  - Provide information about the skills that teacher candidates bring to initial teacher preparation
  - Provide information about their instructional needs
- Results will enable efficient and wise use of time and other resources

# PROGRAM LEVEL ASSESSMENT

UM's redesigned Elementary Undergraduate Teacher Education Program includes program level assessment:

- Focus on high leverage teaching practices, content knowledge for teaching, and professional ethical obligations
- Serve multiple purposes
- Involve and inform core stakeholders
- Infused into the program at multiple points in time
  - Beginning, midpoint, and conclusion of the program
  - Within courses and in designated assessment windows

# ELICITING AND INTERPRETING STUDENT THINKING

**A core teaching practice:** to find out what students know or understand, and how they are thinking/reasoning

- Establishing an environment in which a student is comfortable sharing his/her thinking
- Posing questions to get students to talk
- Listening to and hearing what students say
- Probing students' responses
- Developing an idea of what a student thinks
- Checking one's interpretation

# FOCUSING ON ELICITING AND INTERPRETING FROM THE BEGINNING OF TEACHER EDUCATION

Early attention to eliciting and interpreting student thinking is crucial, because:

- People are likely to develop ways of doing this in everyday life
- Caring about what students think is foundational to teaching
- It is foundational to many other teaching practices

# USING STANDARDIZED SIMULATIONS TO ASSESS ELICITING AND INTERPRETING

- **Efficient:** Standardization allows for the assessment of many teaching candidates in a compressed timeframe
- **Parity:** Makes possible fairness with respect to specific contextual aspects
- **Detail:** Enables specification of content, situation, teaching “problem” to ensure that important aspects of teaching are being assessed



# ① ASSESSING SKILLS WITH THE CORE PRACTICES OF ELICITING AND INTERPRETING CHILDREN'S MATHEMATICAL THINKING



SCHOOL OF  
EDUCATION  
UNIVERSITY OF MICHIGAN



This work is licensed under the Creative Commons Attribution-Noncommercial-No Derivative Works  
Version 3.0 United States License: <http://creativecommons.org/licenses/by-nc-nd/3.0/us/>

© 2015 Mathematics Teaching and Learning to Teach • School of Education • University of Michigan • Ann Arbor, MI 48109 • [mtt@umich.edu](mailto:mtt@umich.edu)

# ASSESSING SKILLS OF ELICITING AND INTERPRETING STUDENT THINKING

## CONTEXT

- **Focus:** Eliciting and interpreting student thinking with particular mathematics content
- **Timing:** Beginning of the program; before coursework focused on eliciting and interpreting student thinking

## ASSESSMENT OVERVIEW

An intern:

- Interacts with a “standardized student” about a sample of student work
- Responds to a series of follow-up questions to surface the intern’s
  - Interpretation of the student’s thinking
  - Hypothesis about how the student would perform on a similar task

# SETTING THE STAGE FOR ELICITING

$$\begin{array}{r} 29 \\ 36 \\ + 18 \\ \hline 623 \\ \textcircled{83} \end{array}$$

The teaching intern:

1. Prepares for an interaction with a standardized student about one piece of student work

Your goal is to elicit and probe to find out what the “student” did to produce the answer as well as the way in which the student understands the steps that were performed.

$$\begin{array}{r} 29 \\ 36 \\ + 18 \\ \hline 623 \\ \textcircled{83} \end{array}$$

Final answer 83

**Correct answer, alternative algorithm, degree of understanding is unclear**

# HOW IS EVIDENCE OF ELICITING SKILLS OBTAINED?

$$\begin{array}{r} 29 \\ 36 \\ + 18 \\ \hline 623 \\ \textcircled{83} \end{array}$$

The teaching intern:

1. Prepares for an interaction with a standardized student about one piece of student work
- 2. Interacts with the student to probes the standardized student's thinking**

## A Standardized Student

Developed response guidelines focused on:

- What the student is thinking, such as
  - Uses an alternative algorithm (column addition), except the student is working from left to right
  - Applies the method correctly and has conceptual understanding of the procedure
- General orientations towards responses such as
  - Talk about digits in columns in terms of the place value of the column (e.g., 23 ones)
  - Give the least amount of information that is still responsive to the question
- Responses to anticipated questions



# ELICITING STUDENT THINKING: VIEWING FOCUS

$$\begin{array}{r} 29 \\ 36 \\ + 18 \\ \hline 623 \\ \textcircled{83} \end{array}$$

**What can we notice about this teaching intern's skill with eliciting student thinking?**

Evaluate whether the teaching intern:

- Launches the interactions with a question that is neutral, open, and focused on student thinking
- Elicits the specific steps of the student's process
- Elicits the student's understanding of the steps
- Attends to the students' ideas in follow-up questions
- Uses appropriate tone and manner

# ELICITING STUDENT THINKING: VIEWING FOCUS

$$\begin{array}{r} 29 \\ 36 \\ + 18 \\ \hline 623 \\ \textcircled{83} \end{array}$$

**What can we notice about this teaching intern's skill with eliciting student thinking?**

Evaluate whether the teaching intern:

- Launches the interactions with a question that is neutral, open, and focused on student thinking
- Elicits the specific steps of the student's process
- Elicits the student's understanding of the steps
- Attends to the students' ideas in follow-up questions
- Uses appropriate tone and manner

# ② SKILLS OF TEACHING INTERNS AT TWO POINTS IN THE PROGRAM



SCHOOL OF  
EDUCATION  
UNIVERSITY OF MICHIGAN



This work is licensed under the Creative Commons Attribution-NonCommercial-No Derivative Works  
Version 3.0 United States License: <http://creativecommons.org/licenses/by-nc-nd/3.0/us/>

© 2015 Mathematics Teaching and Learning to Teach • School of Education • University of Michigan • Ann Arbor, MI 48109 • [mtlt@umich.edu](mailto:mtlt@umich.edu)

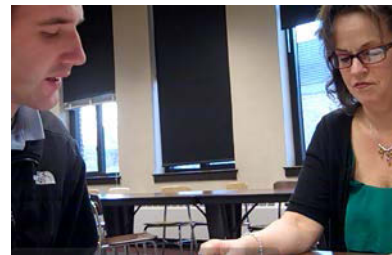
# INITIAL SKILL IN ELICITING STUDENT THINKING

## Context:

- 2013 baseline simulation assessment (48 interns)
- Data collected during the first week of the TE program

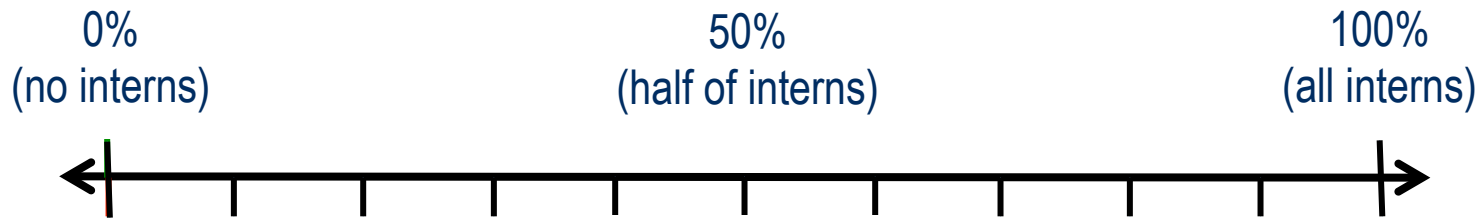
## Analyzing the prevalence of eliciting moves:

- Eliciting components of the student's process
- Probing the student's understanding of the process
- Encouraging and attending to what the student says and writes
- Posing a purposeful follow-up problem





# PREVALENCE OF ELICITING MOVES: PROCESS AND/OR UNDERSTANDING

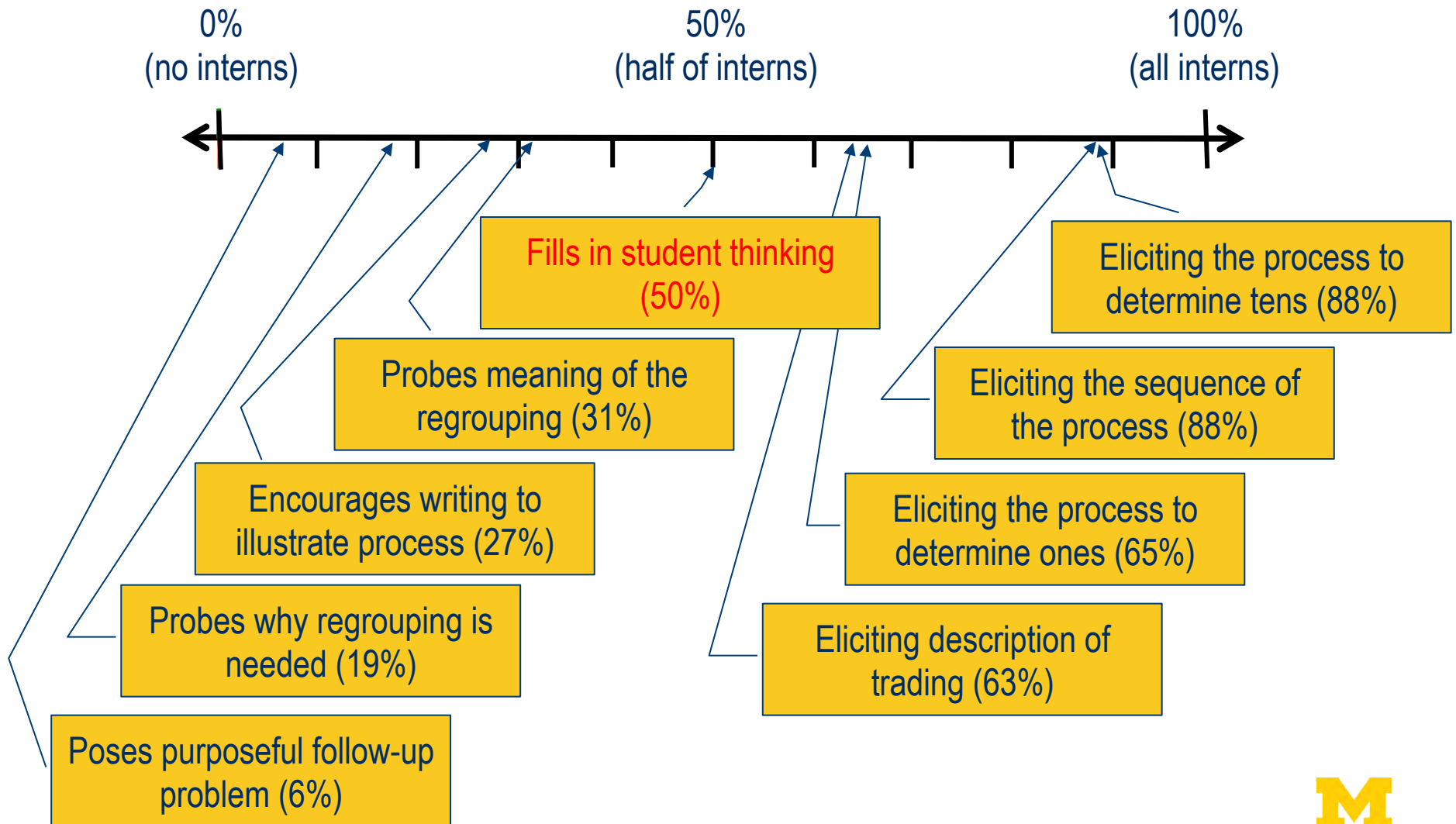


$$\begin{array}{r}
 29 \\
 36 \\
 + 18 \\
 \hline
 623 \\
 \textcircled{83}
 \end{array}$$

Eliciting description of trading	Fills in student thinking	Encourages writing to illustrate process
Eliciting the sequence of the process	Eliciting the process to determine ones	Poses purposeful follow-up problem
Probes why regrouping is needed	Probes meaning of the regrouping	Eliciting the process to determine tens

Which of the moves listed would you expect to see the most often/least often at the beginning of a teacher education program?

# PREVALENCE OF MOVES: POSING A FOLLOW-UP PROBLEM



This work is licensed under the Creative Commons Attribution-Noncommercial-No Derivative Works Version 3.0 United States License: <http://creativecommons.org/licenses/by-nc-nd/3.0/us/>

© 2015 Mathematics Teaching and Learning to Teach • School of Education • University of Michigan • Ann Arbor, MI 48109 • mtl@umich.edu

# ASSESSING SKILLS OF ELICITING AND INTERPRETING STUDENT THINKING (AGAIN)

## CONTEXT

- **Focus:** Eliciting and interpreting student thinking with particular mathematics content
- **Timing:** End of the first year in the program; after coursework focused on eliciting and interpreting student thinking

## ASSESSMENT PROMPT

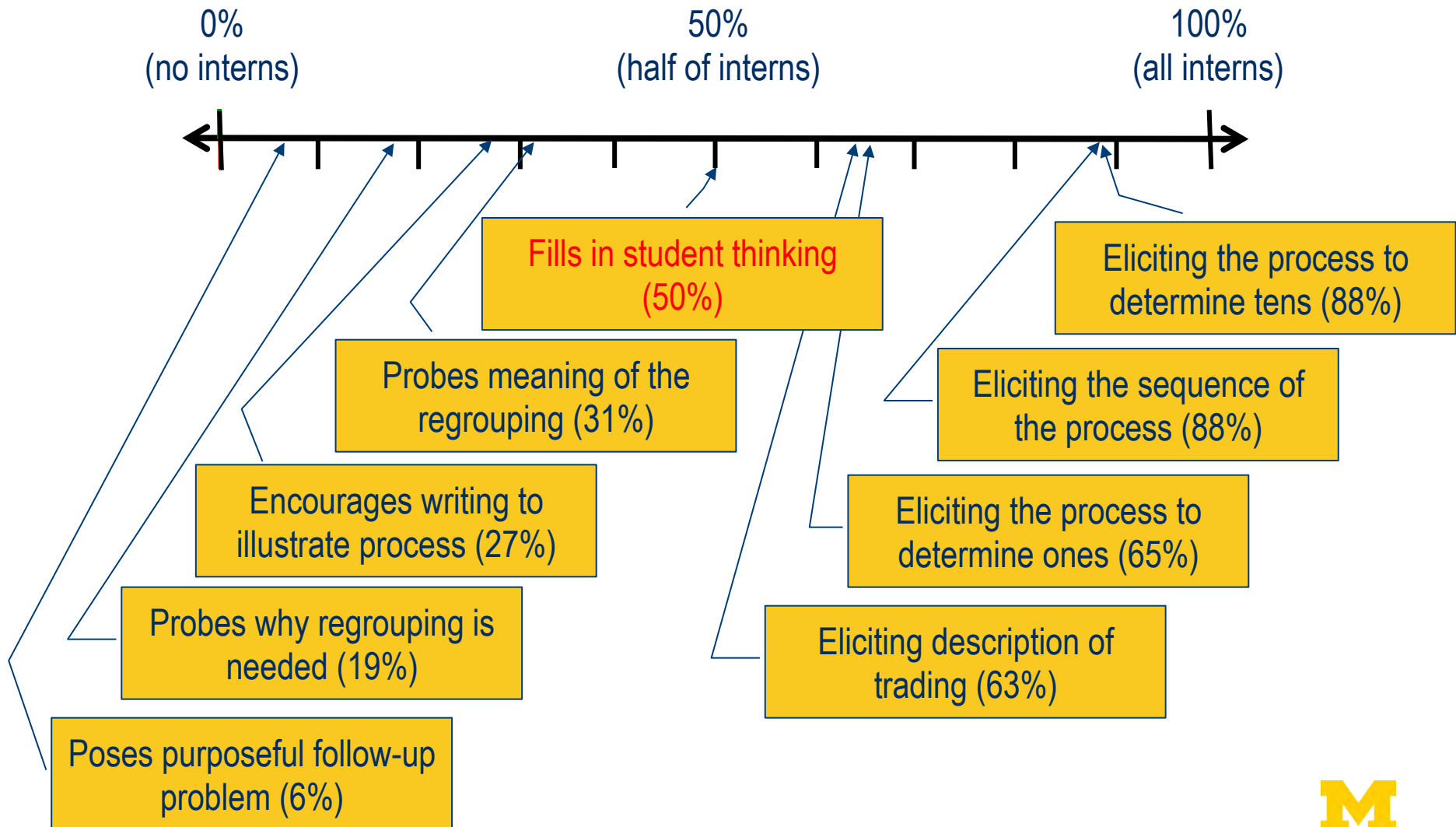
Which fraction is greater:  $\frac{3}{7}$  or  $\frac{2}{5}$

$$\frac{3}{7} = \frac{6}{14} \quad \frac{2}{5} = \frac{6}{15}$$

$$\frac{6}{14} < \frac{6}{15}$$

$$\text{So: } \frac{3}{7} < \frac{2}{5}$$

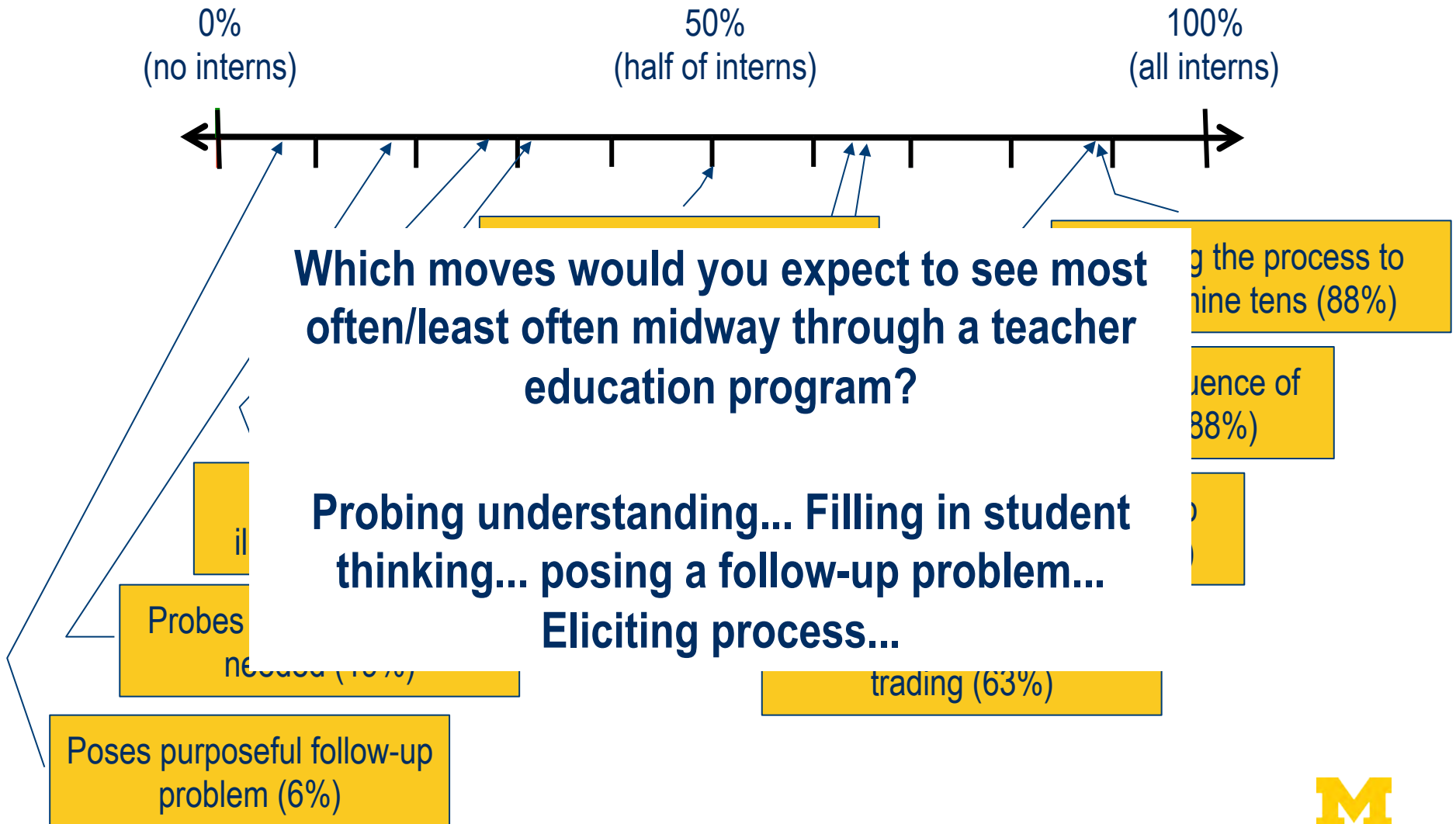
# PREVALENCE OF ELICITING MOVES: BASELINE PERFORMANCE



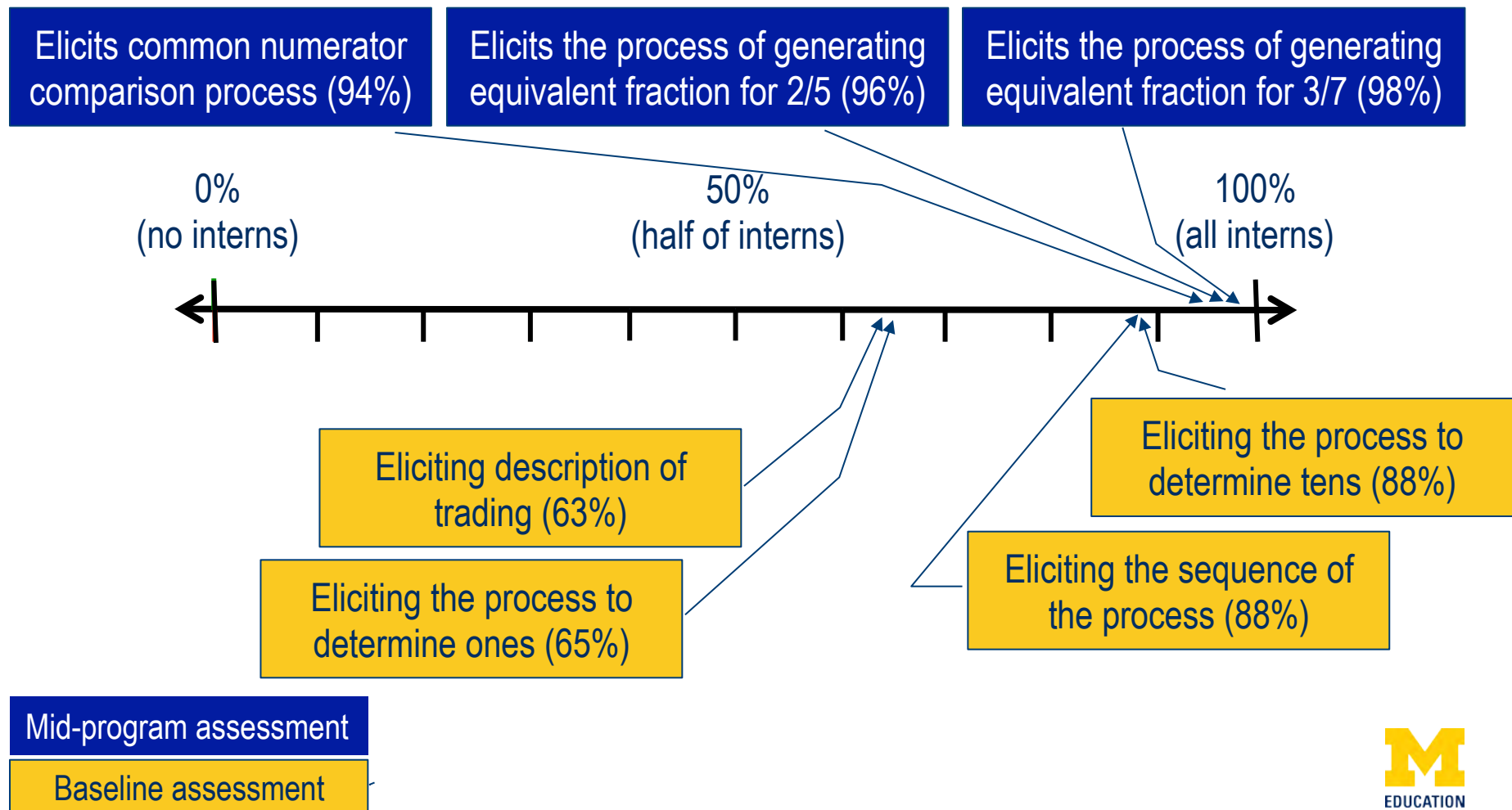
This work is licensed under the Creative Commons Attribution-Noncommercial-No Derivative Works Version 3.0 United States License: <http://creativecommons.org/licenses/by-nc-nd/3.0/us/>

© 2015 Mathematics Teaching and Learning to Teach • School of Education • University of Michigan • Ann Arbor, MI 48109 • mtl@umich.edu

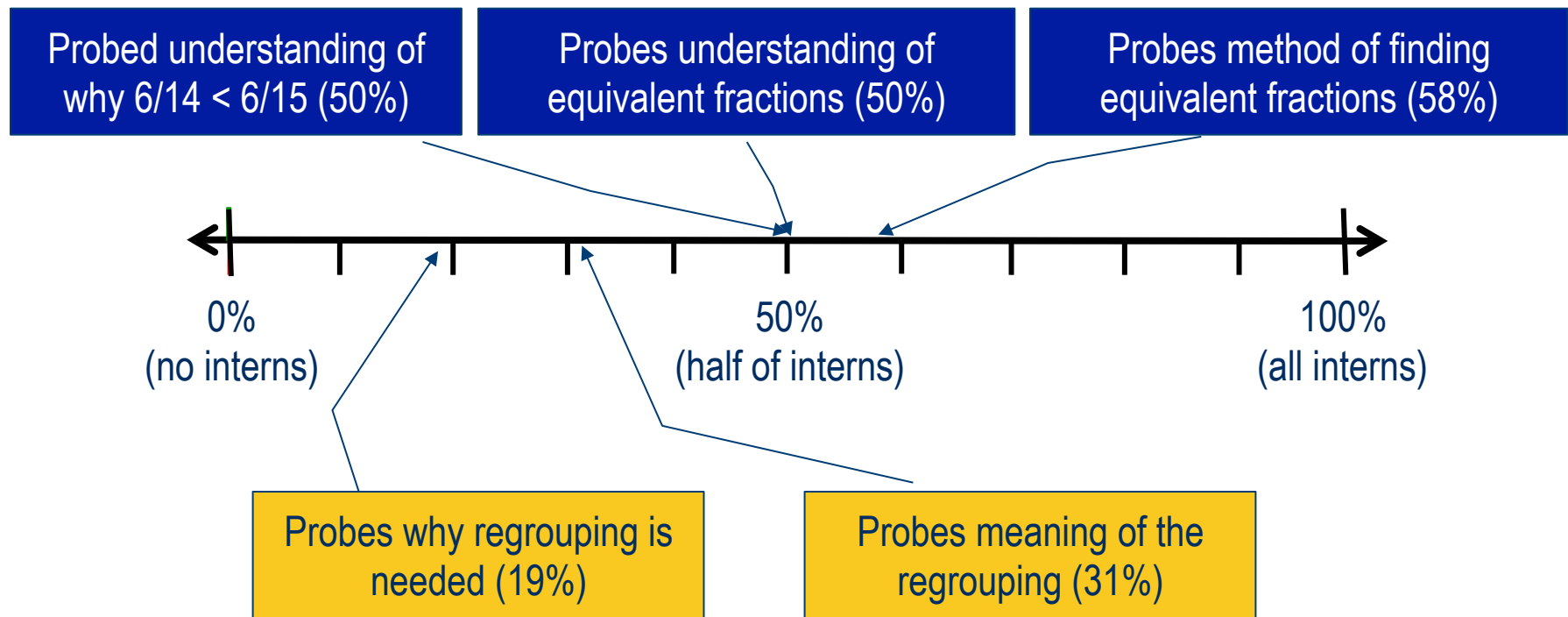
# PREVALENCE OF ELICITING MOVES: BASELINE PERFORMANCE



# PREVALENCE OF ELICITING MOVES: ELICITING PROCESS MID-PROGRAM

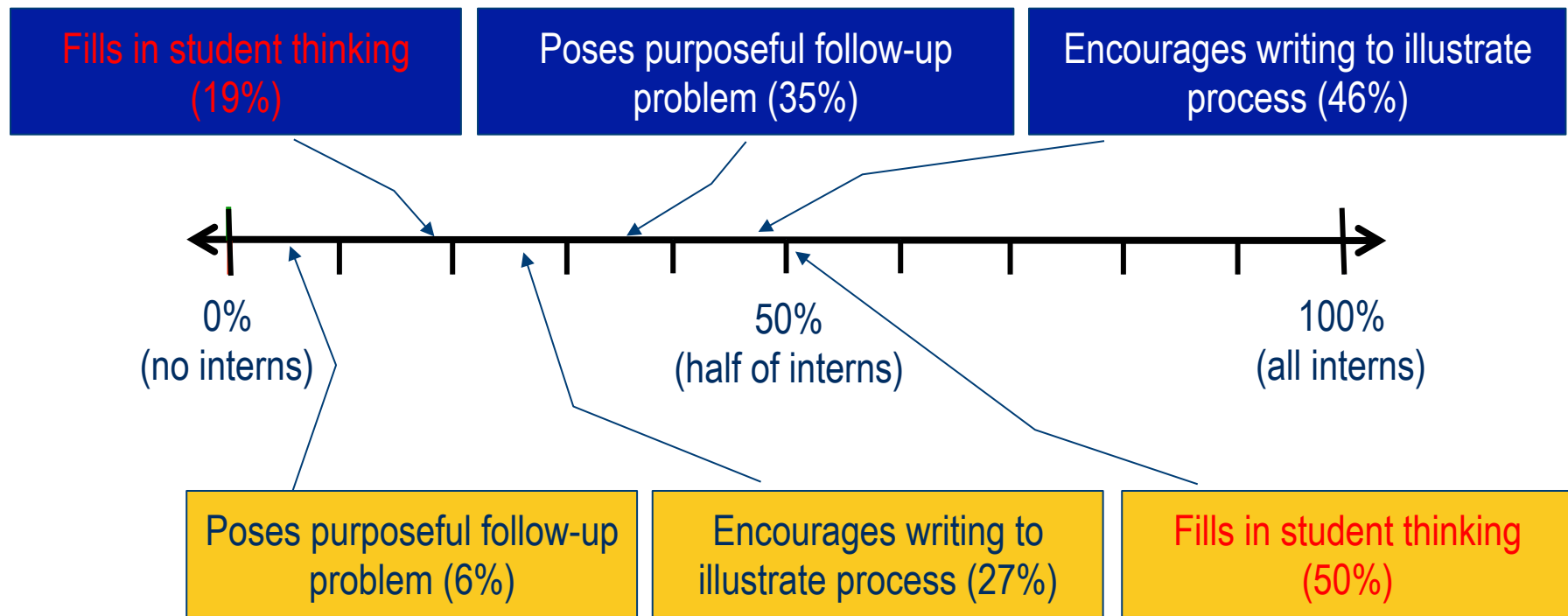


# PREVALENCE OF ELICITING MOVES: ELICITING UNDERSTANDING MID-PROGRAM



This work is licensed under the Creative Commons Attribution-NonCommercial-No Derivative Works Version 3.0 United States License: <http://creativecommons.org/licenses/by-nc-nd/3.0/us/>

# PREVALENCE OF ELICITING MOVES: OTHER ELICITING MOVES MID-PROGRAM



Mid-program assessment  
Baseline assessment



This work is licensed under the Creative Commons Attribution-Noncommercial-No Derivative Works Version 3.0 United States License: <http://creativecommons.org/licenses/by-nc-nd/3.0/us/>

© 2015 Mathematics Teaching and Learning to Teach • School of Education • University of Michigan • Ann Arbor, MI 48109 • [mttt@umich.edu](mailto:mttt@umich.edu)



# ③ SUPPORTING THE DEVELOPMENT OF SKILL WITH ELICITING



SCHOOL OF  
EDUCATION  
UNIVERSITY OF MICHIGAN

# CHILDREN AS SENSE-MAKERS

- Nine-week course focused on developing the following practices:
  - Eliciting and interpreting children’s mathematical thinking
  - Explaining mathematical content, with a focus on fractions
  - Using assessment information to inform instruction
- Course is in the 2<sup>nd</sup> semester of the 4-semester undergraduate elementary program
- Follows a 4-week “Children as Sense-Makers” course, which focuses on eliciting and interpreting children’s thinking in the context of science
- Includes work in a 5<sup>th</sup> grade classroom and in interns’ field placements (3<sup>rd</sup> – 5<sup>th</sup> grade classrooms)

# SEQUENCE OF WORK ON ELICITING

Teaching interns:

1. **Unpack the work of eliciting**
2. Assignment #1: Interview a student in field placement
3. Elicit the thinking of a fifth grade student:
  - Interview about work on a fractions quiz
  - Targeted instruction session
4. Assignment #2: Interview a different student in field placement

## Viewing focus

- What questions does the teacher pose?
- What appears to be the purposes of those questions?
- What does the teacher do to establish an environment that encourages the student to share her thinking?

## Eliciting student thinking

### Observable components:

- Initially eliciting student thinking
- Asking following up questions
  - Probing to learn about a student's understanding of key mathematical ideas
  - Probing to learn about the student's process for solving fractions problems
  - Connecting to the student's thinking
- Establishing a supportive environment
- Maintaining a focus on eliciting student thinking
- Representing mathematics accurately

### Not directly observable components:

- Developing an hypothesis about how the student is reasoning and understanding and checking it

# SEQUENCE OF WORK ON ELICITING

## Teaching interns:

1. Unpack the work of eliciting
2. **Assignment #1: Interview a student in field placement**
3. Elicit the thinking of a fifth grade student:
  - Interview about work on a fractions quiz
  - Targeted instruction session
4. **Assignment #2: Interview a different student in field placement**

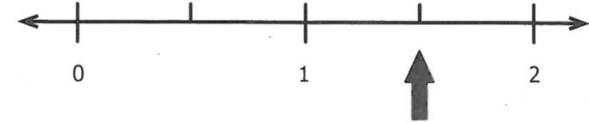


# SEQUENCE OF WORK ON ELICITING

## Teaching interns:

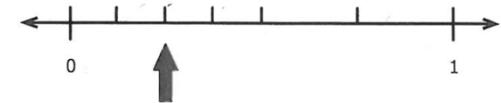
1. Unpack the work of eliciting
2. Assignment #1: Interview a student in field placement
3. **Elicit the thinking of a fifth grade student:**
  - Interview about work on a fractions quiz
  - Targeted instruction session
4. Assignment #2: Interview a different student in field placement

4. Look at the number line below.



What fraction is the big arrow pointing to? 1 1/2

5. Look at the number line below.



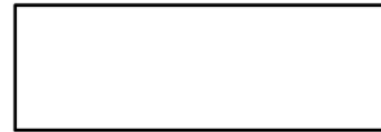
What fraction is the big arrow pointing to? 2/4

# SEQUENCE OF WORK ON ELICITING

## Teaching interns:

1. Unpack the work of eliciting
2. Assignment #1: Interview a student in field placement
3. Elicit the thinking of a fifth grade student:
  - Interview about work on a fractions quiz
  - Targeted instruction session
4. **Assignment #2: Interview a different student in field placement**

1. Shade  $\frac{1}{5}$  of the rectangle.



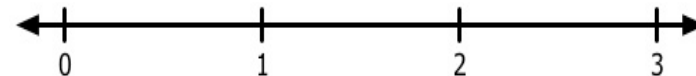
2. Circle the larger fraction.

$$\frac{1}{4} \text{ or } \frac{3}{4}$$

$$\frac{1}{4} \text{ or } \frac{1}{6}$$

$$\frac{4}{4} \text{ or } \frac{4}{8}$$

3. Put the fraction  $\frac{2}{3}$  on the number line.


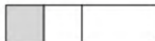



# INTERNS' WORK ON ELICITING IN THE CONTEXT OF INTERVIEW ASSIGNMENTS

Prepare to elicit a student's thinking

AREA #1: Naming a shaded part of area as a fraction

Hypothesis about the student's process and understanding, based on the written work:  
Record your hypothesis here. You will use the hypothesis as you generate questions to confirm/disconfirm your hypothesis.

Problem	Specific questions tied to student's written work	Notes and Reminders
1. What fraction of the rectangle below is shaded red? 		
2. What fraction of the rectangle below is shaded red?  How do you know?		
3. Look at the big rectangle below.  What fraction of the big rectangle is shaded green? What fraction of the big rectangle is shaded blue?		

## Beginning Repertoire of Teacher Questions

### 1) Initial eliciting of students' thinking

- What was your first step in solving this problem?
- Show us your solution and explain your steps.
- Share your [first] step.
- What were your initial thoughts about this problem?
- How did you begin working on this problem?
- Would anyone be willing to explain one of the solutions they found?

### 2) Probing students' answers

- Trying to figure out what a student means or is thinking when you don't understand what he or she is saying
- Checking whether right answers are supported by correct understanding
- Probing wrong answers to understand student thinking
  - Tell us more about that.
  - How did you arrive at that answer?
  - Can you elaborate that?
  - Can you repeat that?
  - What do you mean by

# INTERNS' WORK ON ELICITING IN THE CONTEXT OF INTERVIEW ASSIGNMENTS

Prepare to elicit a student's thinking



Enact the practice of eliciting in the field

**AREA #1: Naming a shaded part of area as a fraction**

*Hypothesis about the student's process and understanding, based on the written work: Record your hypothesis here. You will use the hypothesis as you generate questions to confirm/disconfirm your hypothesis.*

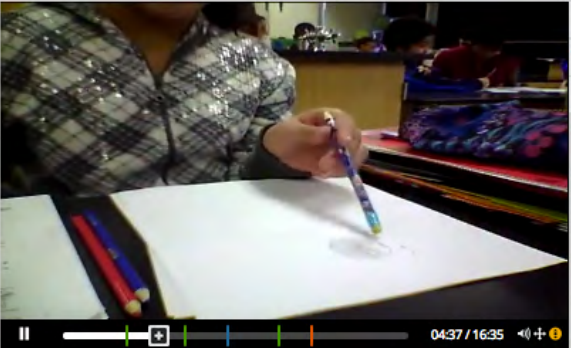
Problem	Specific questions tied to student's written work	Notes and Reminders
1. What fraction of the rectangle is shaded red?		
2. What fraction of the rectangle below is shaded red?		

Beginning Repertoire of Teacher Questions

- 1) **Initial eliciting of students' thinking**
  - What was your first step in solving this problem?
  - Show us your solution and explain your steps.
  - Share your [first] step.
  - What were your initial thoughts about this problem?
  - How did you begin working on this problem?
  - Would anyone be willing to explain one of the solutions they found?
  
- 2) **Probing students' answers**
  - a. **Trying to figure out what a student means or is thinking when you don't understand what he or she is saying**
  - b. **Checking whether right answers are supported by correct understanding**
  - c. **Probing wrong answers to understand student thinking**
    - Tell us more about that.
    - How did you arrive at that answer?
    - Can you elaborate that?
    - Can you repeat that?
    - What do you mean by



# INTERNS' WORK ON ELICITING IN THE CONTEXT OF INTERVIEW ASSIGNMENTS



04:37 / 16:35

Comments 1 Questions 3 Suggestions  
Strengths 1 Notes 0

**03:01** Susanna F. Coach Suggestion  
It might have been helpful here to say WHY the wholes need to be the same size. - a few seconds ago  
Reply

**05:50** Susanna F. Coach Suggestion  
What do you think the student meant by "the lines"? This would have been a good place to probe further. - 21 minutes ago  
Reply

**07:52** Susanna F. Coach Strength  
This question allowed you to learn some important things about what the student was attending to when she was using the diagrams to compare the two fractions. - 16 minutes ago

Prepare to elicit a student's thinking



Enact the practice of eliciting in the field

Analyze the video record of the enactment

AREA #1: Naming a shaded part of area as a fraction


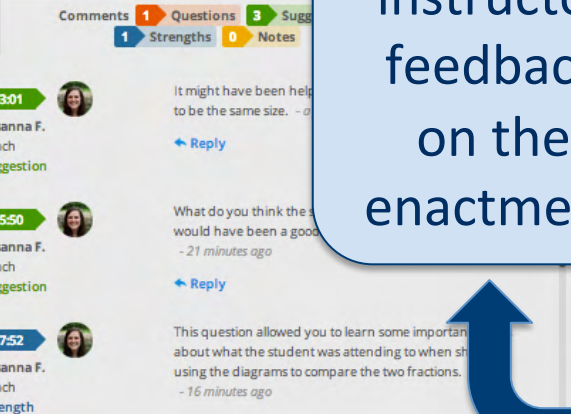
Hypothesis about the student's process and understanding, based on the written work: Record your hypothesis here. You will use the hypothesis as you generate questions to confirm/disconfirm your hypothesis.

Problem	Specific questions tied to student's written work	Notes and Reminders
1. What fraction of the rectangle shaded red?		
2. What fraction of the rectangle below is shaded red?		

- Beginning Repertoire of Teacher Questions
- Initial elicitation of students' thinking
    - What was your first step in solving this problem?
    - Show us your solution and explain your steps.
    - Show us your [first] step.
    - What were your initial thoughts about this problem?
    - When did you begin working on this problem?
    - Who else was willing to explain one of the solutions they found?
  - Probing students' answers
    - Trying to figure out what a student means or is thinking when you don't understand what he or she is saying
    - Checking whether right answers are supported by correct understanding
    - Probing wrong answers to understand student thinking
      - Tell us more about that.
      - How did you arrive at that answer?
      - Can you elaborate that?
      - Can you repeat that?
      - What do you mean by...



# INTERNS' WORK ON ELICITING IN THE CONTEXT OF INTERVIEW ASSIGNMENTS

Comments 1 Questions 3 Sugg  
Strengths 0 Notes

03:01 Susanna F. Coach Suggestion  
It might have been helpful to be the same size. - 0

05:50 Susanna F. Coach Suggestion  
What do you think the student would have been a good at? - 21 minutes ago

07:52 Susanna F. Coach Strength  
This question allowed you to learn some important things about what the student was attending to when she was using the diagrams to compare the two fractions. - 16 minutes ago

Prepare to elicit a student's thinking

Consider instructor feedback on the enactment



Analyze the video record of the enactment

AREA #1: Naming a shaded part of area as a fraction

Hypothesis about the student's process and understanding, based on the written work: Record your hypothesis here. You will use the hypothesis as you generate questions to confirm/disconfirm your hypothesis.

Problem	Specific questions tied to student's written work	Notes and Reminders
1. What fraction of the rectangle is shaded red?		
2. What fraction of the rectangle below is shaded red?		

Enact the practice of eliciting in the field

Beginning Repertoire of Teacher Questions

1) Initial elicitation of students' thinking

- When you see your first step in solving this problem?
- Show us your solution and explain your steps.
- Show us your [first] step.
- What were your initial thoughts about this problem?
- How do you begin working on this problem?
- Who else is willing to explain one of the solutions they found?

2) Probing students' answers

- Trying to figure out what a student means or is thinking when you don't understand what he or she is saying
- Checking whether right answers are supported by correct understanding
- Probing wrong answers to understand student thinking
  - Tell us more about that.
  - How did you arrive at that answer?
  - Can you elaborate that?
  - Can you repeat that?
  - What do you mean by...



# OTHER COURSE FEATURES THAT SUPPORT INTERNS' ELICITING

- Work on relevant mathematics content alongside working on practices of eliciting, including
  - Definition of a fraction
  - Area model and number line representations
  - Strategies for comparing fractions, generating equivalent fractions
  - Fraction computation
- Learn common patterns of student thinking about fractions

# EXAMPLE OF ELICITING AT THE END OF THE COURSE (FINAL INTERVIEW ASSIGNMENT)

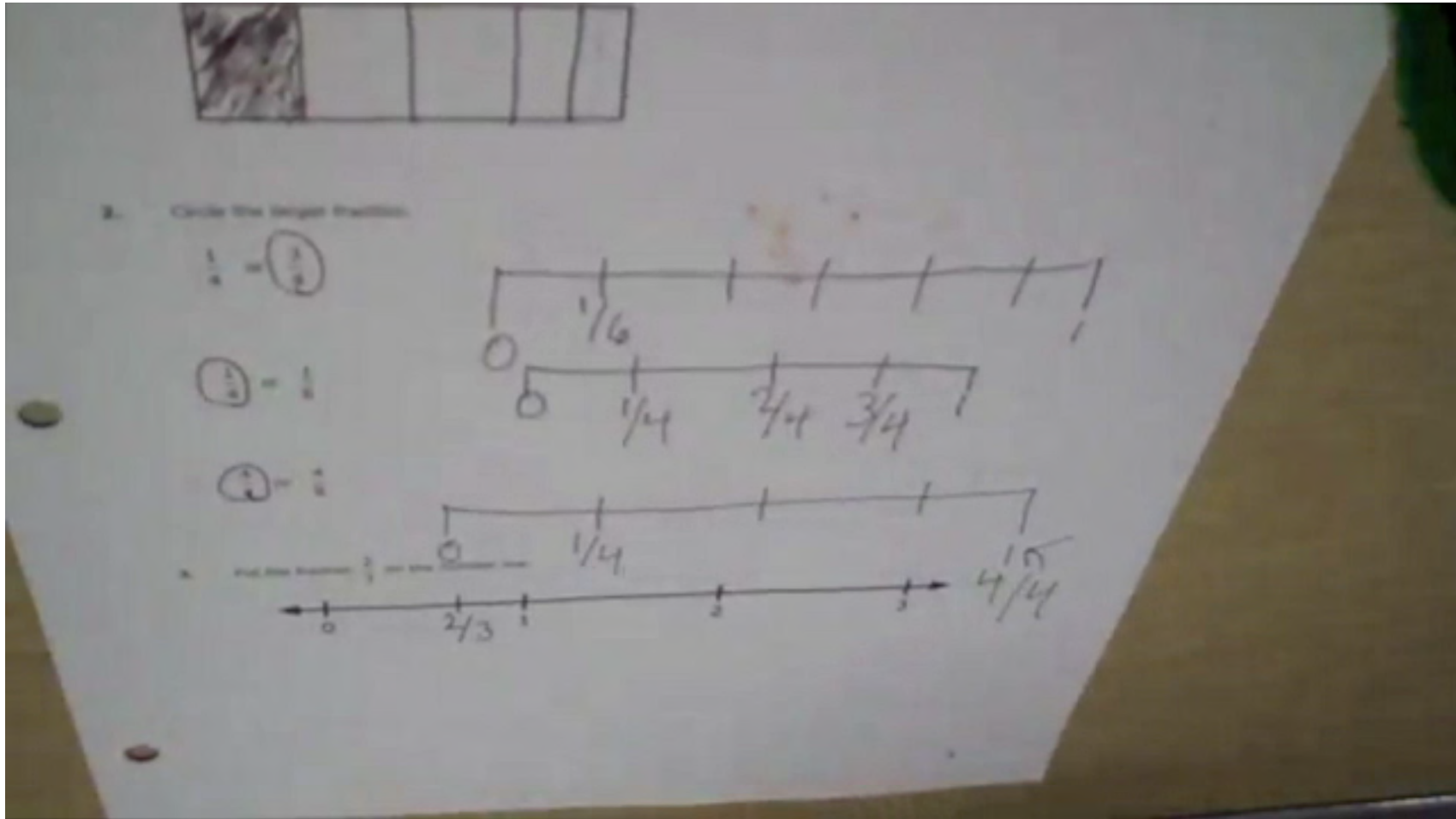
Put the fraction  $\frac{2}{3}$  on the number line.



## Viewing focus:

- What moves does the intern use to
  - Elicit the student's process for marking  $\frac{2}{3}$  on the number line
  - Elicit the student's understanding of the definition of a fraction and the number line representation
- How does the intern attend to the ideas the student shares?

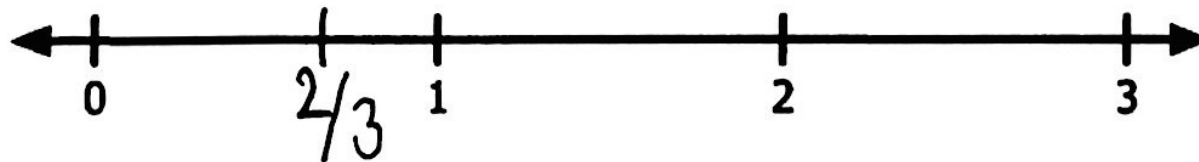
# EXAMPLE OF ELICITING AT THE END OF THE COURSE (FINAL INTERVIEW ASSIGNMENT)





# EXAMPLE OF ELICITING AT THE END OF THE COURSE (FINAL INTERVIEW ASSIGNMENT)

Put the fraction  $\frac{2}{3}$  on the number line.



The intern asks the student to:

- Explain to a classmate
- Place  $2\frac{1}{2}$  on the line

The intern's prompts are evidence that the intern is adjusting to what she is hearing from the student

# ④ NEXT STEPS



SCHOOL OF  
EDUCATION  
UNIVERSITY OF MICHIGAN



This work is licensed under the Creative Commons Attribution-Noncommercial-No Derivative Works  
Version 3.0 United States License: <http://creativecommons.org/licenses/by-nc-nd/3.0/us/>

© 2015 Mathematics Teaching and Learning to Teach • School of Education • University of Michigan • Ann Arbor, MI 48109 • [mtt@umich.edu](mailto:mtt@umich.edu)

# NEXT STEPS: SUPPORTING THE LEARNING OF INTERNS

Instructors can support interns as they:

- Work on particular aspects of their teaching
- Become more discerning about which aspects of student thinking to crucial to probe
- Enhance their skill with eliciting in the context of other teaching practices in subsequent semesters



# NEXT STEPS: ASSESSMENT DEVELOPMENT

- Explore different simulation design features and combinations
  - Changing the student's "way of being"
  - Juxtaposing different mathematical approaches (invented/standard) with different outcomes (correct/incorrect)
- Develop scaffolds for those learning the role of the standardized student
- Develop performance thresholds for different points in teacher development
- Explore different ways of designing simulations
  - Select generative cases of actual student approaches
  - Select from research on student thinking

# NEXT STEPS: RESEARCH

- Validation studies that connect performance in simulations with performance in classroom contexts
- Studies of how different simulation scenarios function (relative difficulty, comparability)
- Studies of the intersection between mathematical knowledge and the practices of eliciting and interpreting