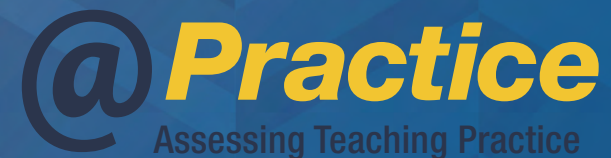


TOWARDS LEARNING TRAJECTORIES FOR CORE PRACTICES IN TEACHER PREPARATION: ELICITING STUDENT THINKING

Sarah Kate Selling, Meghan Shaughnessy, & Timothy Boerst

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TOWARDS LEARNING TRAJECTORIES IN TEACHER EDUCATION

- High-leverage teaching practices in teacher education →
Need to understand more what it means to support new teachers to learn to enact these practices
(e.g., Ball & Forzani, 2009; Grossman et. al., 2009; McDonald et al., 2013)
- Learning trajectories at the K-12 level
(Carpenter et al. 1989; Clements & Sarama, 2014)
- Potential role of learning trajectories for high-leverage practices to inform the design and improvement of teacher preparation

ZOOMING IN ON ONE PRACTICE: ELICITING STUDENT THINKING

To find out what students know or understand, and how they are thinking/reasoning, a teacher must:

- Establish an environment in which a student is comfortable sharing his/her thinking
- Pose questions to get students to talk
- Listen to and hearing what students say
- Probe students' responses
- Develop ideas about what a student thinks
- Check one's interpretation

USING SIMULATIONS TO INVESTIGATE TRAJECTORIES FOR PRACTICE

Simulations are approximations of practice that can be used for both assessing and supporting ongoing learning.

Simulations:

- Place authentic, practice-based demands on a participant
- Purposefully suspend or standardize some elements of the practice-based situation
- Are commonly used in many professional fields
- Can provide insights that are not possible or practical to determine in real-life professional contexts
- Allow for comparisons across time

EXPLORING THE TASK

- Examine the fourth grade student's work
- Anticipate what the student was likely thinking
- Generate questions to ask the student to:
 - Elicit *what* the “student” did to produce the answer
 - Probe what the student *understands* about the process used and the mathematical ideas underlying that process.

$$\begin{array}{r} 78\cancel{4} \\ - 3\cancel{1}5 \\ \hline 469 \end{array}$$

SETTING THE STAGE FOR ELICITING

The preservice teacher:

1. Prepares for an interaction with a standardized student about one piece of student work

$$\begin{array}{r} \boxed{784} \\ - 315 \\ \hline \end{array}$$

Add 10 ones

Your goal is to elicit and probe to find out what the “student” did to produce the answer as well as the way in which the student understands the steps that were performed.

$$\begin{array}{r} 784 \\ - 315 \\ \hline 469 \end{array}$$

Correct answer, alternative algorithm, degree of understanding is unclear

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How can the difference between the two numbers be re-established?

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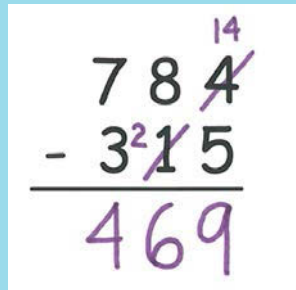
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HOW IS EVIDENCE OF ELICITING SKILLS OBTAINED?

$$\begin{array}{r} 78\cancel{4}^{14} \\ - 3\cancel{1}5 \\ \hline 469 \end{array}$$

The preservice teacher:

1. Prepares for an interaction with a standardized student about one piece of student work
2. **Interacts with the student to probes the standardized student's thinking**



A Standardized Student

Developed response guidelines focused on:

- What the student is thinking such as
 - Uses a method not conventional in the U.S. (but that is standard in many European and South American countries)
 - Applies the method correctly and has conceptual understanding of the procedure
- General orientations towards responses such as
 - Talk about digits in columns in terms of the place value of the column (e.g., 14 ones)
 - Give the least amount of information that is still responsive to the question
- Responses to anticipated questions

ELICITING A STUDENT'S THINKING



METHODS



Context

- Practice-based elementary teacher education program
- Simulation assessment
 - Year 1: Preservice teachers after one semester of the program ($n = 23$)
 - Year 2: Preservice teachers at the end of four semesters ($n = 19$)

Data sources

- Video records of eliciting

FINDINGS:

MATHEMATICAL FOCUS OF THE QUESTIONS

- The Y2 preservice teachers made fewer **connections to the standard algorithm** than Y1 (21% vs. 52%)
- **Persistent questioning** around the standard algorithm by Y1 preservice teachers
 - “Why did do something to the 1 here instead of doing something to the 8?”
 - “If you were to do something to the 8, would you know what to do?”
 - “If you were going to do something to the 8, what would you do?”

Why did you change the 1 instead of the 8?

$$\begin{array}{r} 784 \\ - 315 \\ \hline 469 \end{array}$$

FINDINGS: TIMING, EFFICIENCY, AND FLUENCY

$$\begin{array}{r} 78\overset{14}{4} \\ - 3\overset{2}{1}5 \\ \hline 469 \end{array}$$

On average, Year 1 preservice teachers spent more time eliciting - 208 seconds (Year 1) v. 157 seconds (Year 2)

- Fluency
 - More Y1 preservice teachers had **noticeable pauses**: 35% v. 11%
 - More Y1 preservice teachers had questions which were coded as **“clunky”**: 48% v. 32%
- Inefficient use of time
 - Posing several possibly less strategic problems (e.g., two subtraction and one addition problem)
 - Posing ill-defined tasks (e.g., negative answer, three numbers)
 - Drawing base ten blocks without engaging the student with them

FINDINGS: RESPONSIVENESS TO STUDENT THINKING

$$\begin{array}{r} 784 \\ - 315 \\ \hline 469 \end{array}$$

- Both groups used revoicing and clarifying moves
- Y2 preservice teachers used clarifying moves more often and strategically

Student: Then I crossed out the one and wrote a two.

Preservice teacher: Why did you do that?

Student: I added 10 ones to 784 so I need to add ten to the other number.

Preservice teacher: What other number?

Student: The 315.

Preservice teacher: Okay, and why did you have to add a ten to the other number?

Student: Because if you make one number bigger, you have to do the same thing to the other number to keep the problem the same.

Preservice teacher: And what do you mean by the same?

Student: Like you have to keep the difference between the numbers the same.

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CONCLUSION AND DISCUSSION

- Differences between groups
 - Mathematical focus – standard algorithm
 - Timing and fluency
 - Responsiveness to student thinking
- Simulation allowed for comparisons between groups
- Affordances of using an alternative algorithm to learn about preservice teachers' eliciting

EMERGING QUESTIONS

- What is the role of instruction in these trajectories?
Are some aspects developmental?
- How can simulations help us investigate trajectories?
- What is the role of mathematical knowledge for teaching in learning trajectories for eliciting student thinking? Would it look different around a different scenario with a more familiar algorithm?